

$\leq$

less than or equal to  
no(t) more than  
maximum  
 $\leq 60$   
at most

$\geq$

greater than or equal to  
no(t) less than  
minimum  
at least

open dot

$>$

$<$

closed dot

$\geq$

$\leq$

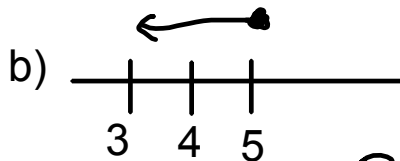
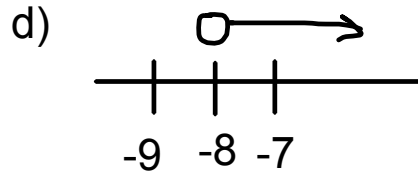
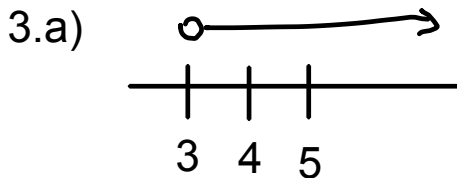
1. a)  $y \leq 25$     b)  $x > y$     c)  $a > 4$     d)  $a + 2 \leq 13$

e)  $2d - 5 \rightarrow e$     f)  $s \leq 100$      ~~$s \geq 100$~~

2. A2    B1    C5 ~~B3~~    E5

C4

$$\begin{array}{r} 100 \\ \downarrow \\ 101 \\ 102 \end{array}$$



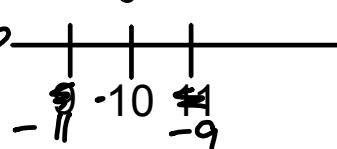
e)  $-2x + 6 \leq 26$

Number line with tick marks at -9, -8, -7. A closed circle is at -10, and an arrow points to the right.



$-2x \leq 26 - 6$   
 $-2x \leq 20$   
 $x \geq 10$

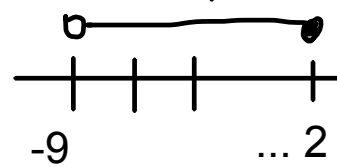
$-2$  (circled)



$x < -\frac{8}{5}$

$-\frac{9}{5}$      $-\frac{8}{5}$      $-\frac{7}{5}$

$]-\infty, -\frac{8}{5}[$



4. a)  $a < c - b + d$

e)  $a + b - d \geq c$

b)  $b < a - c + d$

$a \geq c - b + d$

c)  $a > -\frac{c}{b}$

$-ab < c$ , then

~~$\frac{a}{b} < \frac{c}{-b}$~~

$a > \frac{c}{b}$

$a > \frac{c}{b}$

## Solving Inequalities

$$\left(\frac{2}{3}\right)\left(-\frac{3}{2}\right)x < 5$$

Golden rule: inequalities are flipped when...

multiply/dividing by a negative number

e.g.  $3 - 2x < 5$

$$-2x < 5 - 3$$

$$\frac{2x}{2} < \frac{-2}{2}$$

$$\cancel{+2}x < \frac{2}{-2}$$

$$x > -1$$

e.g.  $3(2-x) + 1 > 2x - 3$

$$6 - 3x + 1 > 2x - 3$$

$$6 - 3x > 2x - 3 - 1$$

$$-3x > 2x - 3 - 1 - 6$$

$$-3x - 2x > -3 - 1 - 6$$

$$\frac{-5x}{-5} > \frac{-10}{-5}$$

$$x < 2$$

$$\rightarrow 7 - 3x > 2x - 3$$

$$7 + 3 > 2x + 3x$$

$$7 + 3 - 3x > 2x$$

$$10 - 3x > 2x$$

$$10 > 2x + 3x$$

$$\frac{10}{5} > \frac{5x}{5}$$

$$2 > x$$

## Inequalities in Word Problems

There is a zombie outbreak in Canada, but so far only two cities have been severely infected. Toronto has twice as many zombies as Montreal, but combined they have at least 600 000 zombies. This means that there are at least how many zombies in Montreal?

$$\begin{array}{r}
 \text{Mt} \quad | \quad \text{Tor} \\
 x \quad + \quad 2x \quad \geq \quad 600\,000 \\
 201000 \quad 3x \geq 600\,000 \\
 200000 \geq x \quad \neq \quad x \geq 200\,000
 \end{array}$$