

p. 107 # 8. Two observations are made concerning a certain number of coins placed on a table. They are described mathematically by the following equations:

$$\rightarrow \underbrace{0.25x + 0.1y + 2}_{\text{amt of money}} = \underbrace{3.5}_{\text{amt of money}}$$

$$\rightarrow x + y + 1 = 10 \rightarrow \# \text{ of coins}$$

a) Describe these observations. i.e. what does each equation represent?

b) How many coins of each denomination are on the table?

$$\textcircled{1} \begin{aligned} 0.25x + 0.1y &= 1.5 \\ x + y &= 9 \end{aligned} \quad \begin{aligned} x &= 9 - y \\ x &= -y + 9 \end{aligned}$$

$$0.25x + 0.1(9 - x) = 1.5$$

$$0.25x + 0.9 - 0.1x = 1.5$$

$$0.15x = 0.6$$

$$x = 4$$

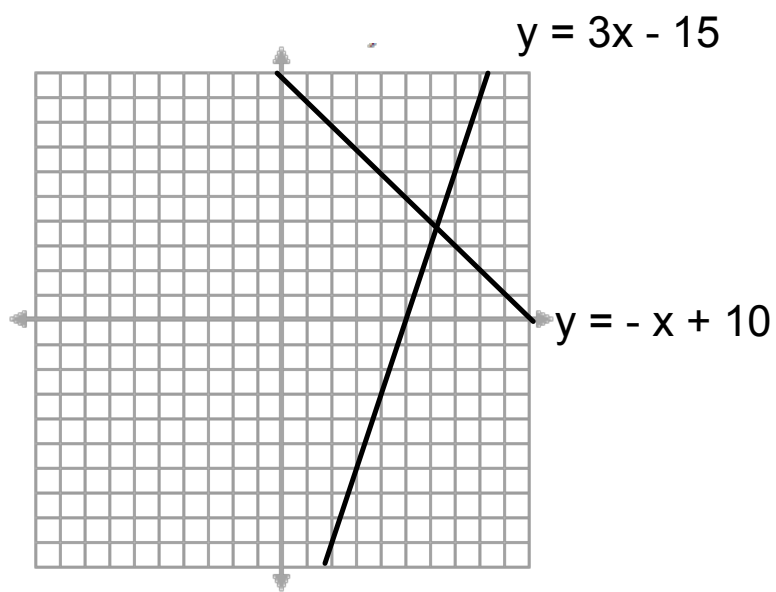
$$y = 9 - 4 = 5$$

$$0.25(9 - y) + 0.1y = 1.5$$

$$2.25 - 0.25y + 0.1y = 1.5$$

$$\frac{9}{4} - \frac{1}{4}y + 0.1y = 1.5$$

5.



Substitution

Plug in your answer into one of the original equations.

Solve.

Plug in (substitute) the expression for the variable in the **other** equation.

Simplify and solve.

Pick an equation and isolate one of the variables.

Elimination

How to solve a system of equations by elimination:

1. Rearrange the equations so that they are in the same order.
2. Multiply one or both equations to get two matching variables.
3. Subtract one equation from the other, **eliminating** one of the variables (be sure to flip all the signs!).
4. Simplify and solve.
5. Plug in and solve again.

e.g. p. 106 #3.b)

$$\begin{array}{r}
 2x - 2y = -8 \\
 - (x + 3y = 2) \\
 \hline
 \cancel{1}x - 5y = -10 \\
 \hline
 \frac{-5y}{-5} = \frac{-10}{-5} \\
 y = 2 \quad \times
 \end{array}$$

$$\begin{array}{r}
 632 \\
 \hline
 111 \\
 \hline
 521
 \end{array}$$

$$\begin{array}{r}
 2x - 2y = -8 \\
 -2(x + 3y = 2) \\
 \hline
 -2x - 6y = -4 \\
 \hline
 \cancel{0} - 8y = -12 \\
 \hline
 \frac{-8y}{-8} = \frac{-12}{-8} \\
 y = 1.5
 \end{array}$$

$$\begin{array}{r}
 \cancel{2x - 2y = -8} \\
 - (x + 3y = 2) \\
 \hline
 \cancel{x} - 5y = -10
 \end{array}$$

$$\begin{array}{r}
 2x - 2(1.5) = -8 \\
 2x - 3 = -8 \\
 2x = -5 \\
 x = -2.5
 \end{array}$$

Recall: Common multiple

number that both smaller numbers can divide into evenly

easy way to find:

